



education

Department:
Education
REPUBLIC OF SOUTH AFRICA

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MATHEMATICS P2

FEBRUARY/MARCH 2010

MEMORANDUM

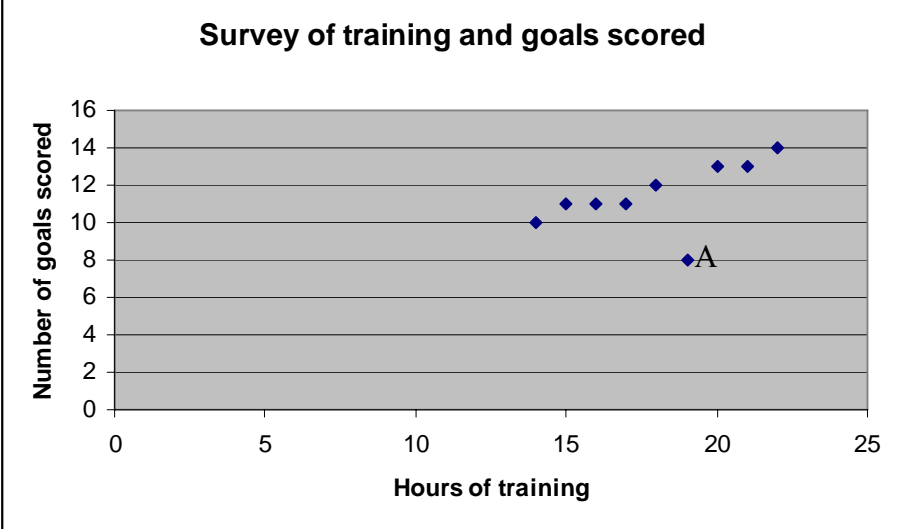
MARKS: 150

This memorandum consists of 14 pages.

QUESTION 1

1.1	Range = $26 - 4 = 22$	✓ maximum and minimum values ✓ answer ANSWER ONLY: Full Marks (2)
1.2	Mean $= \frac{4 + 5 + 8 + 13 + 19 + 22 + 25 + 26 + 23 + 17 + 14 + 7}{12}$ $= \frac{183}{12}$ $= 15,25$	✓ method ✓ 183 ✓ answer (3)
1.3	Standard deviation = 7,6 (7,59522.....)	✓✓ answer (2)
1.4.1	Increase in mean = $\frac{(3 \times 5) + (9 \times 1)}{12}$ $= 2^{\circ}\text{C per month.}$	✓✓ answer (2)
1.4.2	The maximum value increases by 1°C and the minimum value increases by 5°C . This implies that the range of the range of the data will now decrease. This will result in the standard deviation getting smaller. (new SD = 6,27.....)	✓ decrease in range ✓ decrease in standard deviation (2) [11]

QUESTION 2

2.1.1	<p style="text-align: center;">Survey of training and goals scored</p> 	<p>✓✓✓ plotting the points</p> <p>All 9 point correct – 3 marks 5 or 7 points correct – 2 marks 1 or 2 points correct – 1 mark 0 points correct – 0 marks</p> <p style="text-align: right;">(3)</p>
2.1.2	A(indicated on the graph)	<p>✓ answer</p> <p style="text-align: right;">(1)</p>
2.1.3	8 Goals	<p>✓✓ answer</p> <p style="text-align: right;">(2)</p>
2.2	<p>Let the mean time for all 560 learners be x. Then the mean time for the learners living in neighbourhood C is also x.</p> $x = \frac{(135 \times 24) + (225 \times 32) + (200 \times x)}{560}$ $560x = 3240 + 7200 + 200x$ $360x = 10440$ $x = 29$	<p>✓ equal mean times</p> <p>✓ mean \times number</p> <p>✓ simplification</p> <p>✓ answer</p> <p style="text-align: right;">(4) [10]</p>

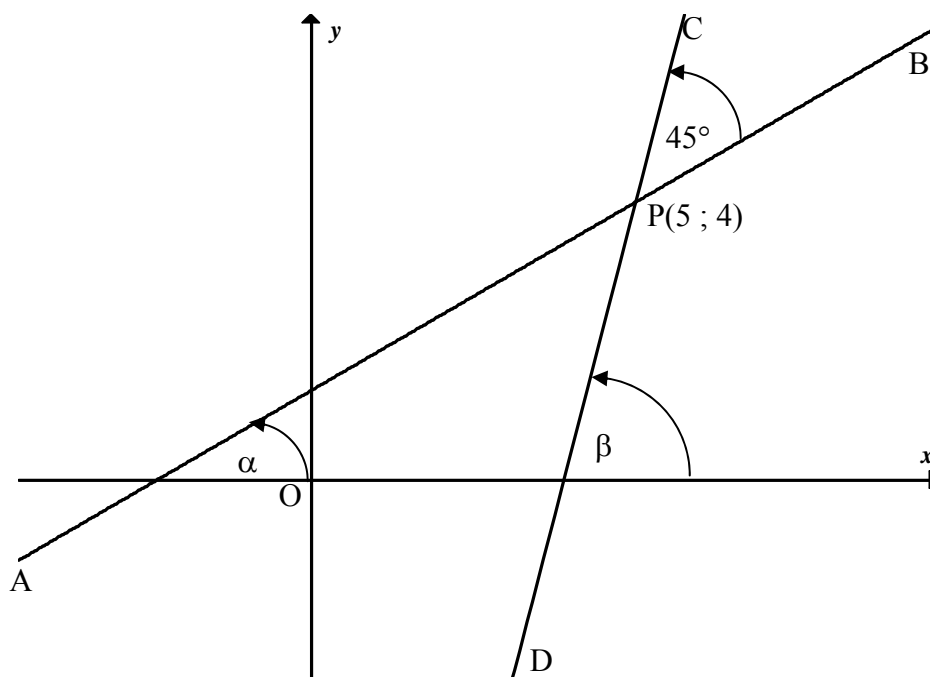
QUESTION 3

<p>3.1</p>	<table border="1"> <thead> <tr> <th>Time (in minutes)</th> <th>$11 \leq t < 15$</th> <th>$15 \leq t < 19$</th> <th>$19 \leq t < 23$</th> <th>$23 \leq t < 27$</th> <th>$27 \leq t < 30$</th> </tr> </thead> <tbody> <tr> <td>Frequency</td> <td>6</td> <td>9</td> <td>13</td> <td>12</td> <td>8</td> </tr> <tr> <td>Cumulative Frequency</td> <td>6</td> <td>15</td> <td>28</td> <td>40</td> <td>48</td> </tr> </tbody> </table>	Time (in minutes)	$11 \leq t < 15$	$15 \leq t < 19$	$19 \leq t < 23$	$23 \leq t < 27$	$27 \leq t < 30$	Frequency	6	9	13	12	8	Cumulative Frequency	6	15	28	40	48	<p>✓ cumulative frequency totals (1)</p>
Time (in minutes)	$11 \leq t < 15$	$15 \leq t < 19$	$19 \leq t < 23$	$23 \leq t < 27$	$27 \leq t < 30$															
Frequency	6	9	13	12	8															
Cumulative Frequency	6	15	28	40	48															
<p>3.2</p>	<p style="text-align: center;">Cumulative Frequency Curve showing the time taken to complete a task</p>	<p>✓✓✓ plotting points at upper limits 6 correct – 3 marks 3 to 5 correct – 2 marks 1 or 2 correct – 1 mark 0 correct – 0 marks ✓ curve (4)</p>																		
<p>3.3</p>	<p>Median value at position 24. Reading off the ogive gives Median \approx 22 minutes LQ value at position 12. Lower quartile \approx 18 minutes (from ogive) UQ value at position 36. Upper quartile \approx 25,5 minutes (from ogive)</p> <p>NOTE: Allow margin of error for reading off the graph.</p>	<p>✓ median ✓ lower quartile ✓ upper quartile (3)</p>																		
<p>3.4</p>		<p>✓ box ✓ whiskers (2)</p>																		
<p>3.5</p>	<p>The times are skewed to the right. A small number of people finished this task very quickly whilst others took more time.</p>	<p>✓ skewed to the right (1) [11]</p>																		

QUESTION 4

4.1	$m_{PQ} = \frac{2-0}{0-4} = -\frac{1}{2}$	✓ substitution (1)
4.2	A: $\left(\frac{0+4}{2}; \frac{2+0}{2}\right)$ A (2 ; 1)	✓ x-coordinate ✓ y-coordinate (2)
4.3	$m_{AB} \cdot m_{PQ} = -1$ $m_{AB} \cdot (-1/2) = -1, \therefore m_{AB} = 2$ Equation of AB is $y = 2x + c$ $\therefore 1 = 2(2) + c$ $c = -3$ Equation of AB is $y = 2x - 3$. OR $m_{AB} \cdot m_{PQ} = -1$ $m_{AB} \cdot (-1/2) = -1, \therefore m_{AB} = 2$ $y - 1 = 2(x - 2)$ $y - 1 = 2x - 4$ $y = 2x - 3$	✓ $m_{AB} \cdot m_{PQ} = -1$ ✓ $m_{AB} = 2$ ✓ equation of AB ✓ $y = 2x - 3$ ✓ $c = -3$ (5) ✓ $m_{AB} \cdot m_{PQ} = -1$ ✓ $m_{AB} = 2$ ✓ gradient of AB ✓ substitution into formula ✓ equation of AB (5)
4.4	B is the point (0 ; -3) $BQ = \sqrt{(0-4)^2 + (-3-0)^2}$ $= 5$	✓ coordinates of B ✓ substitution ✓ answer (3)
4.5	$BP = \sqrt{(0-0)^2 + (-3-2)^2}$ $= 5$ BP = BQ $\therefore \triangle BPQ$ is isosceles. OR BP = 2 + 3 $= 5$ BP = BQ $\therefore \triangle BPQ$ is isosceles	✓ BP = 5 ✓ BP = BQ (2) ✓ BP = 5 ✓ BP = BQ (2)
4.6	If PBQR is a rhombus then A is the midpoint of BR. Let the coordinates of R be (x ; y) $\frac{x+0}{2} = 2$ and $\frac{y-3}{2} = 1$ $x = 4$ $y = 5$ $\therefore R(4 ; 5)$ OR RQ \parallel PB so $x_R = 4$ RQ = PB = 5, so $y_R = 5$ $\therefore R(4 ; 5)$	✓ A is the midpoint of BR ✓ x coordinate ✓ y coordinate (3) ✓ RQ \parallel PB ✓ x coordinate ✓ y coordinate (3) [16]

QUESTION 5



<p>5.1</p> <p>AB is defined as $5y - 3x - 5 = 0$ which can be written as $y = \frac{3}{5}x + 1$</p> <p>$m_{AB} = \frac{3}{5}$</p> <p>Let α be the inclination of AB.</p> <p>$\tan \alpha = \frac{3}{5}$</p> <p>$\alpha = 30,96^\circ$.</p> <p>Let β be the inclination of CD</p> <p>$\beta = 45^\circ + 30,96^\circ$</p> <p>$= 75,96^\circ$</p> <p>Gradient of CD = $\tan 75,96^\circ = 4$.</p> <p>OR</p> <p>$\tan \beta = \tan(\alpha + 45^\circ)$</p> $= \frac{\tan \alpha + \tan 45^\circ}{1 - \tan \alpha \cdot \tan 45^\circ}$ $= \frac{\frac{3}{5} + 1}{1 - \frac{3}{5} \times 1}$ $= 4$ <p>$m_{CD} = \tan \beta$</p> <p>$m_{CD} = 4$</p>	<p>$\checkmark m_{AB} = \frac{3}{5}$</p> <p>$\checkmark \tan \alpha = \frac{3}{5}$</p> <p>$\checkmark \alpha = 30,96^\circ$</p> <p>$\checkmark \beta = 75,96^\circ$</p> <p>$\checkmark$ gradient of CD</p> <p style="text-align: right;">(5)</p> <p>\checkmark expansion</p> <p>$\checkmark \tan 45^\circ = 1$</p> <p>$\checkmark \tan \alpha = \frac{3}{5}$</p> <p>$\checkmark$ substitution</p> <p>\checkmark answer</p> <p style="text-align: right;">(5)</p>
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5.2	<p>Equation of CD is $y = 4x + c$ $\therefore 4 = 4(5) + c$ $c = -16$ Equation of CD is $y = 4x - 16$.</p> <p>OR</p> <p>$y - 4 = 4(x - 5)$ $y - 4 = 4x - 20$ $y = 4x - 16$</p>	<p>✓ y- intercept ✓ equation of CD (2)</p> <p>✓ substitution ✓ equation of CD (2)</p> <p>[7]</p>
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QUESTION 6

6.1	<p>$x^2 + y^2 + 8x + 4y - 38 = 0$ $x^2 + 8x + 16 + y^2 + 4y + 4 = 16 + 4 + 38$ $(x + 4)^2 + (y + 2)^2 = 58$ Centre is $(-4 ; -2)$ and the radius is $\sqrt{58}$</p>	<p>✓ completing the square (both or one) ✓ factor form ✓ centre ✓ radius (4)</p>
6.2	<p>Centre of second circle is $(4 ; 6)$ Distance between centres is $\sqrt{(4 + 4)^2 + (6 + 2)^2} = \sqrt{128} = 11,31$</p>	<p>✓ centre ✓ distance (2)</p>
6.3	<p>Sum of radii = $\sqrt{58} + \sqrt{26} = 12,71$ Distance between centres is 11,31. sum of the radii > distance between the centres \therefore the circles must overlap and hence the circles must intersect.</p>	<p>✓✓ sum of radii ✓ conclusion (3)</p>
6.4	<p>Equation of second circle: $(x - 4)^2 + (y - 6)^2 = 26$ $x^2 - 8x + 16 + y^2 - 12y + 36 = 26$ $x^2 - 8x + y^2 - 12y + 26 = 0$</p> <p>Let $(x ; y)$ be either of the two points on intersection. Then $x^2 + y^2 + 8x + 4y - 38 = 0$ and $x^2 + y^2 - 8x - 12y + 26 = 0$</p> <p>Subtract $\frac{\quad}{\quad}$ $16y + 16x - 64 = 0$ $y = -x + 4$</p> <p>Both points of intersection lie on this line. $\therefore y = -x + 4$ is the equation of the common chord.</p> <p>OR</p>	<p>✓ equation of circle in form = 0 ✓ statement – two points of intersection ✓ subtracting ✓ simplification (4)</p>

	<p>Check that the line $y = -x + 4$ cuts the two circles at the same points:</p> $(x - 4)^2 + (-x - 2)^2 = 26$ $x^2 - 8x + 16 + x^2 + 4x + 4 = 26$ $2x^2 - 4x - 6 = 0$ $x^2 - 2x - 3 = 0$ $(x - 3)(x + 1) = 0$ $x = 3 \text{ or } x = -1$ $x^2 + y^2 + 8x + 4y - 38 = 0$ $x^2 + (4 - x)^2 + 8x + 4(4 - x) - 38 = 0$ $x^2 + 16 - 8x + x^2 + 8x + 16 - 4x - 38 = 0$ $2x^2 - 4x - 6 = 0$ $x^2 - 2x - 3 = 0$ $x = 3 \text{ or } x = -1$	<p>✓ substitution</p> <p>✓ answer</p> <p>✓ substitution</p> <p>✓ answer</p> <p style="text-align: right;">(4)</p> <p style="text-align: right;">[13]</p>
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QUESTION 7

7.1.1	$P'(5; -2)$	<p>✓ answer</p> <p style="text-align: right;">(1)</p>
7.1.2	$P'(5; 2)$	<p>✓ x coordinate</p> <p>✓ y coordinate</p> <p style="text-align: right;">(2)</p>
7.2.1	$K \rightarrow K'' : (14; 4) \rightarrow (2; 2)$ $U \rightarrow U'' : (18; 6) \rightarrow (3; 9)$ $H \rightarrow H'' : (16; 8) \rightarrow (4; 8)$ $L \rightarrow L'' : (18; 10) \rightarrow (5; 9)$ $E \rightarrow E'' : (14; 12) \rightarrow (6; 7)$ So “halve” and ‘interchange” or ‘interchange” and “halve”. Reflection across $y = x$ followed by contraction by $\frac{1}{2}$ OR Contraction by $\frac{1}{2}$ followed by reflection across $y = x$.	<p>✓ reflected</p> <p>✓ the line $y = x$</p> <p>✓ enlarged</p> <p>✓ scale factor of $\frac{1}{2}$</p> <p style="text-align: right;">(4)</p>
7.2.2	$H' = \frac{1}{2}(16; 8) = (8; 4)$ OR $H'(8; 16)$	<p>✓ (8 ; 4)</p> <p>✓ (8 ; 16)</p> <p style="text-align: right;">(2)</p>
7.2.3	Area KUHLE : Area $K''U''H''L''E'' = \left(\frac{2}{1}\right)^2 = 4 : 1$	<p>✓ ✓ answer</p> <p style="text-align: right;">(2)</p> <p style="text-align: right;">[11]</p>

QUESTION 8

<p>8.1</p>	<p>For anti-clockwise rotation:</p> $x' = x \cos \theta - y \sin \theta$ $= 3 \cos 120^\circ - 2 \sin 120^\circ$ $= 3(-\cos 60^\circ) - 2 \sin 60^\circ$ $= 3\left(-\frac{1}{2}\right) - 2\left(\frac{\sqrt{3}}{2}\right)$ $= \frac{-3 - 2\sqrt{3}}{2}$ $y' = x \sin \theta + y \cos \theta$ $= 3 \sin 120^\circ + 2 \cos 120^\circ$ $= 3 \sin 60^\circ + 2(-\cos 60^\circ)$ $= 3\left(\frac{\sqrt{3}}{2}\right) + 2\left(-\frac{1}{2}\right)$ $= \frac{3\sqrt{3} - 2}{2}$ $P\left(\frac{-3 - 2\sqrt{3}}{2}; \frac{3\sqrt{3} - 2}{2}\right)$	<p>✓ formula</p> <p>✓ simplification ✓ substitution</p> <p>✓ answer</p> <p>✓ simplification</p> <p>✓ answer</p> <p>(6)</p>
<p>8.2</p>	$-2 = x\left(-\frac{1}{2}\right) - y\left(\frac{\sqrt{3}}{2}\right)$ $-4 = -x - \sqrt{3}y \quad \dots\dots \text{equation 1}$ $0 = x\left(\frac{\sqrt{3}}{2}\right) + y\left(-\frac{1}{2}\right)$ $0 = \sqrt{3}x + y$ $y = -\sqrt{3}x \quad \dots\dots \text{equation 2}$ <p>Substitute equation 2 into equation 1</p> $-4 = -x - \sqrt{3}(-\sqrt{3}x)$ $-4 = -x + 3x$ $-4 = 2x$ $x = -2$ $y = 2\sqrt{3}$ $Q(-2; 2\sqrt{3})$	<p>✓ $-4 = -x - \sqrt{3}y$</p> <p>✓ $y = -\sqrt{3}x$</p> <p>✓ x-coordinate ✓ y-coordinate</p> <p>(4) [10]</p>

QUESTION 10

10.1.1	$\sin 48^\circ = \sin(36^\circ + 12^\circ)$ $= \sin 36^\circ \cos 12^\circ + \cos 36^\circ \sin 12^\circ$ $= p + q$	✓ writing 48° in terms of 36° and 12° ✓ expansion ✓ answer (3)
10.1.2	$\sin 24^\circ = \sin(36^\circ - 12^\circ)$ $= \sin 36^\circ \cos 12^\circ - \cos 36^\circ \sin 12^\circ$ $= p - q$ <p>OR</p> $\sin 24^\circ = \sin(36^\circ - 12^\circ)$ $= \sin 36^\circ \cos 12^\circ - \cos 36^\circ \sin 12^\circ$ $= p - q$	✓ writing 24° in terms of 36° and 12° ✓ expansion ✓ $\sin 24^\circ = p - q$ (3) ✓ writing 24° in terms of 36° and 12° ✓ expansion ✓ $\sin 24^\circ = p - q$ (3)
10.1.3	$\sin 48^\circ = 2 \sin 24^\circ \cos 24^\circ$ $\therefore p + q = 2(p - q) \cos 24^\circ$ $\therefore \cos 24^\circ = \frac{p + q}{2(p - q)}$ <p>OR</p> $\cos 48^\circ = 2 \cos^2 24^\circ - 1$ $\therefore \cos 24^\circ = \sqrt{\frac{1 + \cos 48^\circ}{2}} = \sqrt{\frac{1}{2} \left(1 + \sqrt{1 - \sin^2 48^\circ} \right)}$ $= \sqrt{\frac{1}{2} \left(1 + \sqrt{1 - (p + q)^2} \right)}$ <p>OR</p> $\cos^2 24^\circ = 1 - \sin^2 24^\circ$ $\cos^2 24^\circ = 1 - (p - q)^2$ $\cos 24^\circ = \sqrt{1 - (p - q)^2}$	✓ $\cos 48^\circ = 2 \cos^2 24^\circ - 1$ ✓ $\sin 48^\circ = p + q$ ✓ answer (3) ✓ $\cos 48^\circ = 2 \cos^2 24^\circ - 1$ ✓ $\sin 24^\circ = p - q$ ✓ answer (3) ✓ $\cos^2 24^\circ = 1 - \sin^2 24^\circ$ ✓ $\sin 24^\circ = p - q$ ✓ answer (3)

<p>10.2</p>	$\begin{aligned} & \sin^2 20^\circ + \sin^2 40^\circ + \sin^2 80^\circ \\ &= \sin^2 20^\circ + (\sin(60^\circ - 20^\circ))^2 + (\sin(60^\circ + 20^\circ))^2 \\ &= \sin^2 20^\circ + (\sin 60^\circ \cos 20^\circ - \cos 60^\circ \sin 20^\circ)^2 + (\sin 60^\circ \cos 20^\circ + \cos 60^\circ \sin 20^\circ)^2 \\ &= \sin^2 20^\circ + \left(\frac{\sqrt{3}}{2} \cos 20^\circ - \frac{1}{2} \sin 20^\circ\right)^2 + \left(\frac{\sqrt{3}}{2} \cos 20^\circ + \frac{1}{2} \sin 20^\circ\right)^2 \\ &= \sin^2 20^\circ + \frac{3}{4} \cos^2 20^\circ - \frac{\sqrt{3}}{2} \cos 20^\circ \sin 20^\circ + \frac{1}{4} \sin^2 20^\circ + \frac{3}{4} \cos^2 20^\circ \\ &\quad + \frac{\sqrt{3}}{2} \cos 20^\circ \sin 20^\circ + \frac{1}{4} \sin^2 20^\circ \\ &= \sin^2 20^\circ + \frac{3}{2} \cos^2 20^\circ + \frac{1}{2} \sin^2 20^\circ \\ &= \frac{3}{2} (\sin^2 20^\circ + \cos^2 20^\circ) \\ &= \frac{3}{2} \end{aligned}$ <p>OR</p> <p>Use $\sin^2 \theta = \frac{1 - \cos 2\theta}{2}$</p> <p><i>LHS</i></p> $\begin{aligned} &= \frac{3}{2} - \frac{1}{2} \{(\cos 40^\circ + \cos 80^\circ) + \cos 160^\circ\} \\ &= \frac{3}{2} - \frac{1}{2} \{(\cos 60^\circ \cdot \cos 40^\circ + \sin 60^\circ \sin 40^\circ + \cos 60^\circ \cdot \cos 40^\circ - \sin 60^\circ \sin 40^\circ) + \cos 160^\circ\} \\ &= \frac{3}{2} - \frac{1}{2} \{(2 \cos 60^\circ \cos 20^\circ) - \cos 20^\circ\} \\ &= \frac{3}{2} - \frac{1}{2} \left\{ \left(2 \times \frac{1}{2} \cos 20^\circ \right) - \cos 20^\circ \right\} \\ &= \frac{3}{2} - 0 \\ &= \frac{3}{2} \end{aligned}$	<p>✓40°= 60° - 20° ✓80°= 60° + 20°</p> <p>✓ ✓expansions ✓ substitution</p> <p>✓ simplification ✓ factorisation</p> <p>(7)</p> <p>✓40°= 60° - 20° ✓80°= 60° + 20°</p> <p>✓ expansion of cos 40° ✓ expansion of cos 60° ✓ simplification ✓ simplification ✓ answer for bracket</p> <p>(7)</p>
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10.3.1	$\frac{\sin^4 x + \sin^2 x \cos^2 x}{1 + \cos x}$ $= \frac{\sin^2 x(\sin^2 x + \cos^2 x)}{1 + \cos x}$ $= \frac{\sin^2 x}{1 + \cos x}$ $= \frac{1 - \cos^2 x}{1 + \cos x}$ $= \frac{(1 - \cos x)(1 + \cos x)}{(1 + \cos x)}$ $= 1 - \cos x$	<p>✓ factorisation</p> <p>✓ $\sin^2 x + \cos^2 x = 1$</p> <p>✓ identity</p> <p>✓ factorisation</p> <p>(4)</p>
10.3.2	$1 + \cos x = 0$ $\cos x = -1$ $x = 180^\circ + k.360^\circ; k \in Z$ Undefined for $x = 180^\circ + k.360^\circ; k \in Z$.	<p>✓ $1 + \cos x = 0$</p> <p>✓ $180^\circ + k.360^\circ$</p> <p>(2)</p> <p>[22]</p>

QUESTION 11

11.1	$1 + \sin x = \cos 2x$ $1 + \sin x = 1 - 2 \sin^2 x$ $\sin x + 2 \sin^2 x = 0$ $\sin x(1 + 2 \sin x) = 0$ $\sin x = 0 \quad \text{or} \quad \sin x = -\frac{1}{2},$ $x = k.180 \quad \text{or} \quad x = -30^\circ + k.360 \quad k \in Z$ $x = 210^\circ + k.360$ $x \in \{180^\circ; 210; 330^\circ; 360^\circ\}$ OR $1 + \sin x = \cos 2x$ $1 + \sin x = \cos^2 x - \sin^2 x$ $1 + \sin x = 1 - \sin^2 x - \sin^2 x$ $\sin x + 2 \sin^2 x = 0$ $\sin x(1 + 2 \sin x) = 0$ $\sin x = 0 \quad \text{or} \quad \sin x = -\frac{1}{2},$ $x = k.180 \quad \text{or} \quad x = -30^\circ + k.360 \quad k \in Z$ $x = 210^\circ + k.360$ $x \in \{180^\circ; 210; 330^\circ; 360^\circ\}$	<p>✓ expansion</p> <p>✓ factorisation</p> <p>✓ equations</p> <p>✓ $x = k.180$</p> <p>✓ solution for $\sin x = -\frac{1}{2}$</p> <p>✓✓ answers</p> <p>(7)</p> <p>✓ expansion</p> <p>✓ factorisation</p> <p>✓ equations</p> <p>✓ $x = k.180$</p> <p>✓ solution for $\sin x = -\frac{1}{2}$</p> <p>✓✓ answers</p> <p>(7)</p>
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<p>11.2</p>		<p> $1 + \sin x$ ✓ max and min values ✓ shape $\cos 2x$ ✓ amplitude ✓ intercepts </p> <p style="text-align: right;">(4)</p>
<p>11.3</p>	<p>$180^\circ \leq x \leq 210^\circ$ or $330^\circ \leq x \leq 360^\circ$</p>	<p>✓✓✓ answer</p> <p style="text-align: right;">(3) [14]</p>

QUESTION 12

<p>12.1</p>	$\frac{b}{\sin[180^\circ - (\alpha + \beta)]} = \frac{BC}{\sin \alpha}$ $BC \sin(\alpha + \beta) = b \sin \alpha$ $BC = \frac{b \sin \alpha}{\sin(\alpha + \beta)}$ <p>but $BC = DF$</p> $\therefore DF = \frac{b \sin \alpha}{\sin(\alpha + \beta)}$ $\cos \theta = \frac{DF}{DE}$ $\therefore DE = \frac{DF}{\cos \theta}$ $\therefore DE = \frac{b \sin \alpha}{\sin(\alpha + \beta) \cos \theta}$	<p> ✓ sine rule ✓ $\hat{A}BC = 180^\circ - (\alpha + \beta)$ ✓ $BC = \dots$ ✓ $BC = DF$ ✓ manipulation ✓ $DE = \dots$ </p> <p style="text-align: right;">(6)</p>
<p>12.2</p>	$DE = \frac{2000 \sin 43^\circ}{\sin 79^\circ \cdot \cos 27^\circ}$ $= 1559,50 \text{ m}$	<p> ✓ substitution numerator ✓ substitution denominator ✓ answer </p> <p style="text-align: right;">(3) [9]</p>

TOTAL: 150