



**education**

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Department:  
Education  
**REPUBLIC OF SOUTH AFRICA**

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P1**

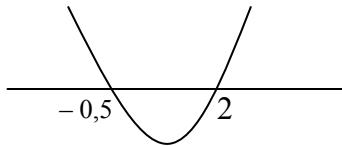
**FEBRUARY/MARCH 2010**

**MEMORANDUM**

**MARKS: 150**

**This memorandum consists of 19 pages.**

**QUESTION 1**

<p>1.1.1</p>	$(x-3)(x+5) = 9$ $x^2 + 2x - 15 = 9$ $x^2 + 2x - 24 = 0$ $(x+6)(x-4) = 0$ $x = 4 \text{ or } x = -6$	<p>✓ expansion ✓ standard form ✓ factorisation ✓ answers</p> <p style="text-align: right;">(4)</p>										
<p>1.1.2</p>	$2x^2 - 3x - 2 \leq 0$ $(2x+1)(x-2) \leq 0$ <p>Critical values : <math>-\frac{1}{2}</math> and 2</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="padding: 0 10px;">+</td> <td style="padding: 0 10px;">0</td> <td style="padding: 0 10px;">-</td> <td style="padding: 0 10px;">0</td> <td style="padding: 0 10px;">+</td> </tr> <tr> <td colspan="2" style="border-top: 1px solid black; border-bottom: 1px solid black; padding: 0 10px;">-0,5</td> <td colspan="2" style="border-top: 1px solid black; border-bottom: 1px solid black; padding: 0 10px;">2</td> <td></td> </tr> </table> <div style="text-align: center; margin: 10px 0;">  </div> $-\frac{1}{2} \leq x \leq 2$	+	0	-	0	+	-0,5		2			<p>✓ factors ✓ critical values</p> <p style="text-align: right;">✓✓ answer (4)</p>
+	0	-	0	+								
-0,5		2										
<p>1.2</p>	$y = -2x - 2 \dots\dots\dots(1)$ $-2x^2 + 8xy + 42 = y \dots\dots\dots(2)$ $-2x^2 + 8x(-2x - 2) + 42 = -2x - 2$ $-2x^2 - 16x^2 - 16x + 42 + 2x + 2 = 0$ $-18x^2 - 14x + 44 = 0$ $9x^2 + 7x - 22 = 0$ $(9x - 11)(x + 2) = 0$ $\therefore x = \frac{11}{9} \quad \text{or} \quad x = -2$ $\therefore y = -2\left(\frac{11}{9}\right) - 2 \quad \therefore y = -2(-2) - 2$ $\therefore y = -\frac{40}{9} \quad \therefore y = 2$ <p><b>OR</b></p>	<p>✓ <math>y = -2x - 2</math></p> <p>✓ substitution</p> <p>✓ simplification</p> <p>✓ factors</p> <p>✓ answers for <math>x</math></p> <p style="text-align: right;">✓✓ answers for <math>y</math> (7)</p>										

<p> <math>y = -2x - 2 \dots\dots\dots(1)</math>  <math>-2x^2 + 8xy + 42 = y \dots\dots\dots(2)</math> </p> <p> <math>y = -2(x+1) = \frac{-2(x^2 - 21)}{1 - 8x}</math>  <math>\therefore (x+1)(1 - 8x) = x^2 - 21</math>  <math>x - 8x^2 + 1 - 8x = x^2 - 21</math>  <math>9x^2 + 7x - 22 = 0</math>  <math>(9x - 11)(x + 2) = 0</math>  <math>\therefore x = \frac{11}{9} \quad \text{or} \quad x = -2</math>  <math>\therefore y = -2\left(\frac{11}{9}\right) - 2 \quad \therefore y = -2(-2) - 2</math>  <math>\therefore y = -\frac{40}{9} \quad \therefore y = 2</math> </p> <p><b>OR</b></p> <p> <math>y = -2x - 2 \dots\dots\dots(1)</math>  <math>-2x^2 + 8xy + 42 = y \dots\dots\dots(2)</math> </p> <p> <math>x = \frac{(-y - 2)}{2}</math>  <math>-2\left(\frac{(-y - 2)}{2}\right)^2 + 8y\left(\frac{(-y - 2)}{2}\right) + 42 - y = 0</math>  <math>-2\left(\frac{y^2 + 4y + 4}{4}\right) + 4y(-y - 2) + 42 - y = 0</math>  <math>y^2 + 4y + 4 + 8y^2 + 16y - 84 + 2y = 0</math>  <math>9y^2 + 22y - 80 = 0</math>  <math>(y - 2)(9y + 40) = 0</math>  <math>y = 2 \quad \text{or} \quad y = -\frac{40}{9}</math> </p> <p> <math>x = -2 \quad \text{or} \quad x = \frac{11}{9}</math> </p>	<p>                 ✓ equating                  ✓ simplification                  ✓ standard form                  ✓ factors                  ✓ answers for x                    ✓✓ answers for y (7)             </p> <p>                 ✓ <math>x = \frac{(-y - 2)}{2}</math>                  ✓ substitution                    ✓ simplification                  ✓ factors                  ✓ answers for y                    ✓✓ answers for x (7)             </p>
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1.3	$g(x) = x^2$ $g(9) = 81$ $f(x) = \sqrt{4x}$ $f(g(9)) = f(81) = \sqrt{4(81)}$ $= 2(9)$ $= 18$ <p><b>OR</b></p> $g(9) = 9^2$ $\therefore f(g(9)) = \sqrt{2^2 \cdot 9^2} = 18$ <p><b>OR</b></p> $f(g(x)) = \sqrt{4g(x)}$ $= \sqrt{4x^2}$ $= 2x$ $f(g(9)) = 2(9)$ $= 18$	<p>✓ <math>g(9) = 81</math></p> <p>✓ substitution</p> <p>✓ answer (3)</p> <p>✓ <math>g(9) = 9^2</math></p> <p>✓ substitution</p> <p>✓ answer (3)</p> <p>✓</p> <p><math>f(g(x)) = \sqrt{4g(x)}</math></p> <p>✓ substitution</p> <p>✓ answer (3)</p>
1.4	$\frac{14}{\sqrt{63} - \sqrt{28}}$ $= \frac{14}{3\sqrt{7} - 2\sqrt{7}}$ $= \frac{14}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}}$ $= 2\sqrt{7}$ <p><math>a = 2</math> and <math>b = 7</math></p> <p>But <math>2\sqrt{7} = \sqrt{28}</math></p> <p>So <math>a = 1</math> and <math>b = 28</math> is also a solution.</p>	<p>✓ simplification</p> <p>✓ simplification</p> <p>✓ rationalising the denominator</p> <p>✓ answer (4)</p> <p>[22]</p>



	<p>The sequence is <math>20^2 - 1 ; 19^2 - 1 ; 18^2 - 1 ; 17^2 - 1 ; \dots\dots</math></p> $T_1 = 20^2 = (20 - 0)^2 - 1$ $T_2 = 19^2 = (20 - 1)^2 - 1$ $T_3 = 18^2 = (20 - 2)^2 - 1$ $T_n = (20 - (n - 1))^2 - 1 = (21 - n)^2 - 1$	<p>✓✓ rewriting terms as squares ✓✓✓ establishing that <math>T_n = (20 - (n - 1))^2</math> ✓ <math>T_n = (21 - n)^2</math></p> <p>(6)</p>
2.2	$n^2 - 42n + 440 = 0$ $(n - 22)(n - 20) = 0$ <p><math>n = 22</math> and <math>n = 20</math> both terms 22 and 20 have values of 0.</p> <p><b>OR</b></p> $(21 - n)^2 - 1 = 0$ $21 - n = 1 \text{ or } -1$ $n = 20 \text{ or } n = 22$	<p>✓ equation</p> <p>✓✓ answers (3)</p> <p>✓ equation</p> <p>✓✓ answers (3)</p>
2.3	$n = \frac{-(-42)}{2(1)}$ $n = 21$ <p>At the 21<sup>st</sup> term, the lowest value is obtained.</p> <p><b>OR</b></p> $2n - 42 = 0$ $2n = 42$ $n = 21$ <p>∴ At the 21<sup>st</sup> term, the lowest value is obtained.</p> <p><b>OR</b></p> $T_n = (21 - n)^2 - 1 ∴$ <p>For <math>n = 21</math>, <math>T_n = (21 - n)^2 - 1 = (21 - 21)^2 - 1 = -1</math> For <math>n = 21</math>, the lowest value (= -1) is obtained.</p>	<p>✓ answer (1)</p> <p>✓ answer (1)</p> <p>✓ answer (1)</p> <p><b>[10]</b></p>

**QUESTION 3**

<p>3.1</p>	<p>Let</p> $S_n = a + ar + ar^2 + ar^3 + \dots + ar^{n-1} \quad (1)$ <p>Then</p> $r \times S_n = r(a + ar + ar^2 + ar^3 + \dots + ar^{n-1})$ $= ar + ar^2 + ar^3 + \dots + ar^n + ar^n \quad (2)$ <p>(2) – (1) gives:</p> $rS_n - S_n = ar^n - a$ $S_n(r - 1) = a(r^n - 1)$ $S_n = \frac{a(r^n - 1)}{(r - 1)}$	<p>✓ writing <math>S_n</math> as a series</p> <p>✓ writing <math>r.S_n</math> as a series</p> <p>✓ subtracting</p> <p>✓ removing common factors</p> <p>(4)</p>
<p>3.2</p>	$a = 3; r = \frac{1}{3}$ $S_\infty = \frac{a}{1 - r}$ $= \frac{3}{1 - \frac{1}{3}}$ $= \frac{9}{2}$	<p>✓ <math>r = \frac{1}{3}</math></p> <p>✓ substitution</p> <p>✓ answer</p> <p>(3) [7]</p>

**QUESTION 4**

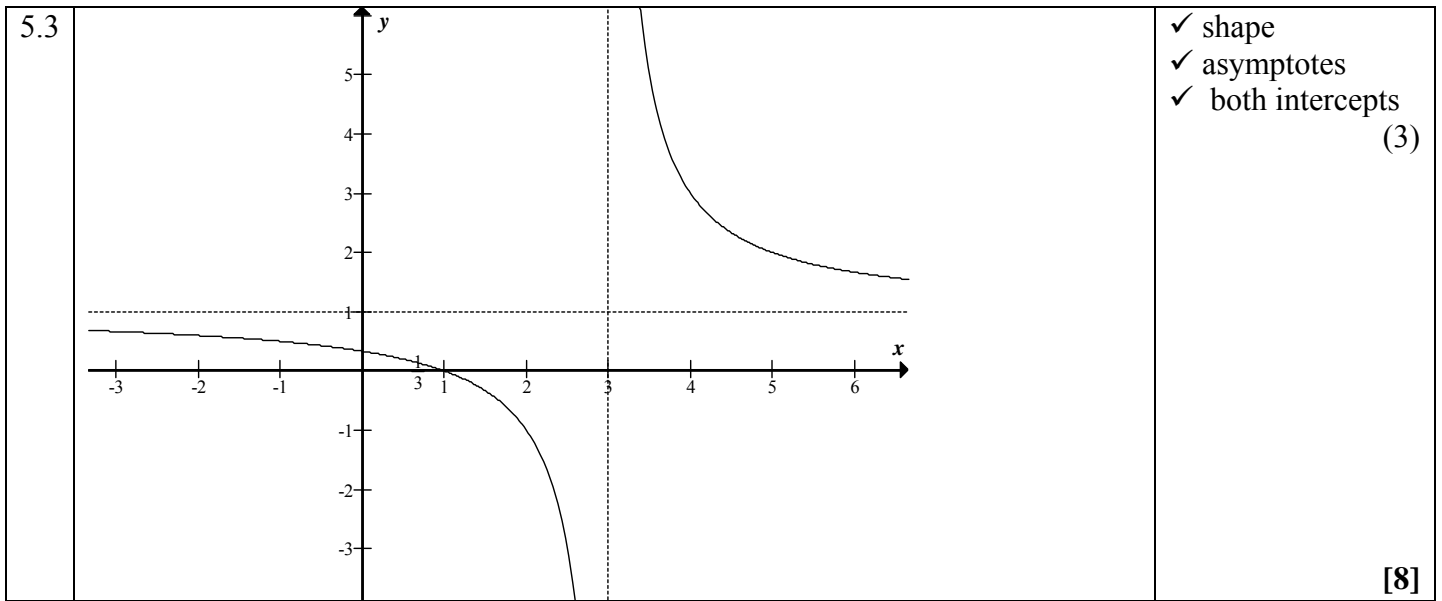
<p>4.1</p>	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 10%;">Term</th> <th style="width: 20%;">Income</th> <th style="width: 20%;">Expenses</th> <th style="width: 20%;">Savings</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>120 000</td> <td>90 000</td> <td>30 000</td> </tr> <tr> <td>2</td> <td>132 000</td> <td>105 000</td> <td>27 000</td> </tr> <tr> <td>3</td> <td>144 000</td> <td>120 000</td> <td>24 000</td> </tr> </tbody> </table> <p><math>30\,000 + 27\,000 + 24\,000 + \dots + 0.</math></p>	Term	Income	Expenses	Savings	1	120 000	90 000	30 000	2	132 000	105 000	27 000	3	144 000	120 000	24 000	<p>✓ 30 000</p> <p>✓ 27 000</p> <p>✓ 24 000</p> <p>✓ series</p> <p>(4)</p>
Term	Income	Expenses	Savings															
1	120 000	90 000	30 000															
2	132 000	105 000	27 000															
3	144 000	120 000	24 000															
<p>4.2</p>	<p>Savings = Income – Expenses</p> <p>Income in year <math>n = 120\,000 + 12\,000(n - 1)</math></p> <p>Expenses in year <math>n = 90\,000 + 15\,000(n - 1)</math></p> $120\,000 + 12\,000(n - 1) = 90\,000 + 15\,000(n - 1)$ $30\,000 + 12\,000n - 12\,000 = 15\,000n - 15\,000$ $33\,000 = 3\,000n$ $n = 11$ <p>∴ After 11 years.</p> <p><b>OR</b></p>	<p>✓✓ equating</p> <p>✓ answer</p> <p>(3)</p>																

	$a = 30\,000$ $d = -3000$  $T_n = 30000 + (n-1)(-3000)$ $0 = 30000 - 3000n + 3000$ $3000n = 33000$ $\therefore n = 11$ $\therefore$ After 11 years	$\checkmark\checkmark$ equation  $\checkmark$ answer  (3)
4.3	$120000 + 12000(25-1) = 90000 + x(25-1)$ $x = 13250$	$\checkmark$ equating  $\checkmark$ answer  (2) <b>[9]</b>

**QUESTION 5**

5.1	$y = 1$ $x = 3$	$\checkmark$ answer $\checkmark$ answer  (2)	
5.2	$\frac{2}{0-3} + 1$ $= \frac{1}{3}$ $y\text{-int} \left( 0; \frac{1}{3} \right)$ $x\text{-int: } 0 = \frac{2}{x-3} + 1$ $0 = 2 + (x-3)$ $1 = x$ $(1; 0)$	$y = \frac{x-1}{x-3}$ $\therefore f(0) = \frac{1}{3}$  $f(x) = 0$ $\Rightarrow x-1 = 0$ $\Rightarrow x = 1$	$\checkmark$ answer  $\checkmark$ substitution $y = 0$  $\checkmark$ answer  (3)

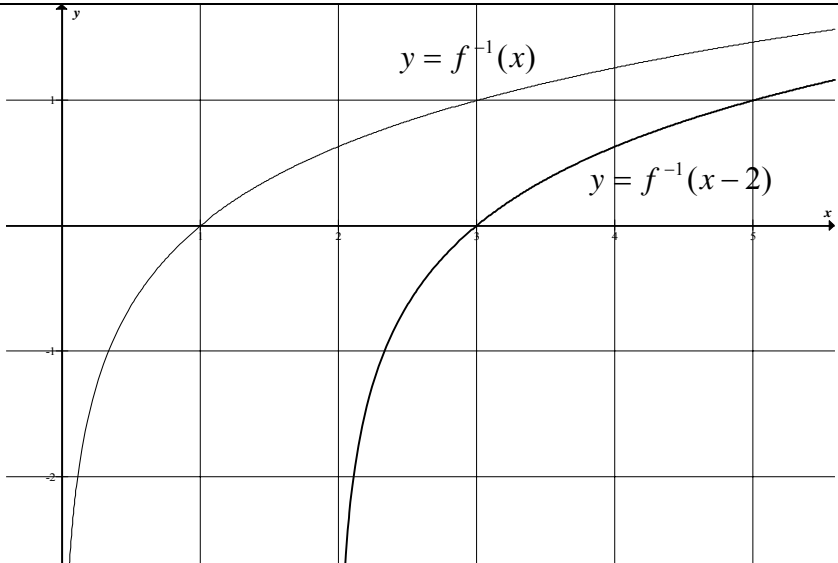




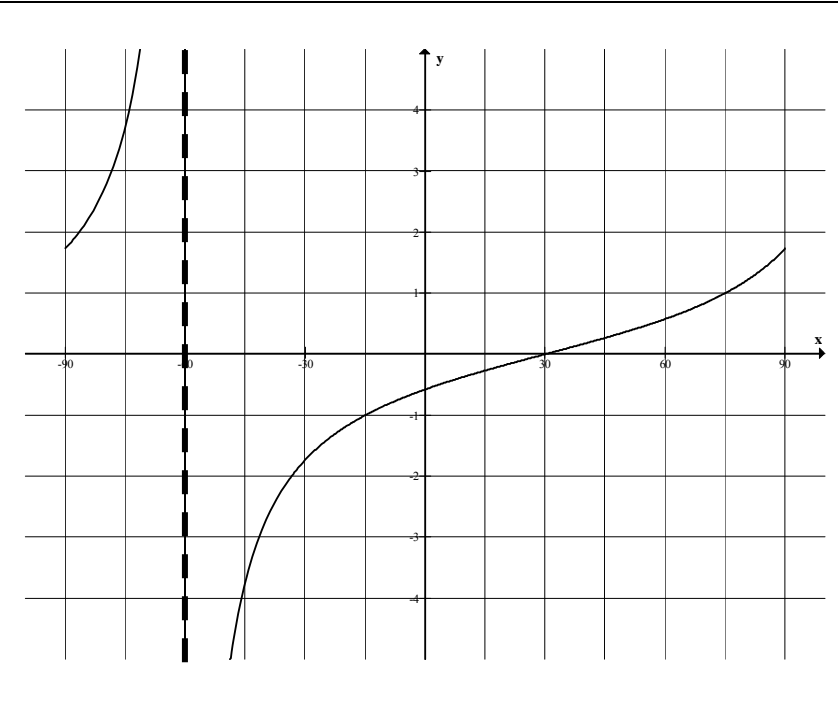
**QUESTION 6**

6.1	$-x^2 + 7x + 8 = 0$ $x^2 - 7x - 8 = 0$ $(x - 8)(x + 1) = 0$ $x = 8 \text{ or } x = -1$ <p>A(-1 ; 0) B(8 ; 0)</p>	<ul style="list-style-type: none"> <li>✓ = 0</li> <li>✓ factors</li> <li>✓ answer A</li> <li>✓ answer B</li> </ul> <p style="text-align: right;">(4)</p>
6.2	$-x^2 + 7x + 8 = -3x + 24$ $-x^2 + 10x - 16 = 0$ $x^2 - 10x + 16 = 0$ $(x - 8)(x - 2) = 0$ $x = 8 \text{ or } x = 2$ <p>x-value of D is 2. (i.e. <math>a = 2</math>)</p>	<ul style="list-style-type: none"> <li>✓ equating</li> <li>✓ standard form</li> <li>✓ factors</li> <li>✓ answer</li> </ul> <p style="text-align: right;">(4)</p>
6.3	$ST = (-x^2 + 7x + 8) - (-3x + 24)$ $= -x^2 + 10x - 16$	<ul style="list-style-type: none"> <li>✓ subtraction</li> <li>✓ answer</li> </ul> <p style="text-align: right;">(2)</p>
6.4	<p>Maximum length of ST is at <math>x = \frac{-10}{2(-1)} = 5</math>.</p> <p>Maximum length of ST is <math>-5^2 + 50 - 16 = 9</math>.</p> <p><b>OR</b></p> <p>Maximum length of ST is <math>\frac{4(-1)(-16) - 10^2}{4(-1)} = 9</math></p>	<ul style="list-style-type: none"> <li>✓ method</li> <li>✓ answer</li> <li>✓ method</li> <li>✓ answer</li> </ul> <p style="text-align: right;">(2)</p>
<b>[12]</b>		

**QUESTION 7**

7.1	$y = \log_3 x$	✓ answer (1)
7.2		$y = f^{-1}(x)$ ✓ x-intercept ✓ shape  $y = f^{-1}(x-2)$ ✓ x-intercept ✓ shape  (4)
7.3	$2 < x < 5$	✓✓ answer (2) [7]

**QUESTION 8**

8.1		✓ shape ✓ x-intercept ✓ vertical asymptote  (3)
8.2	$x = -60^\circ$	✓ answer (1)
8.3	$\tan(30^\circ - x) = -\tan(x - 30^\circ)$ Reflection about the x-axis	✓ reflection ✓ x-axis  (2) [6]

**QUESTION 9**

9.1.1	<p>Total amount = <math>P(1 + in)</math>  <math>= 55\,000(1 + 0,1275(4))</math>  <math>= 83\,050</math></p> <p>Monthly instalment = <math>\frac{83050}{4 \times 12}</math>  <math>= R\,1730,21</math></p>	<p>✓ substitution into simple interest formula          ✓ answer          ✓ <math>\div 48</math></p> <p>✓ answer (4)</p>
9.1.2	$55000 = \frac{x \left[ 1 - \left( 1 + \frac{0,2}{12} \right)^{-12 \times 4} \right]}{\frac{0,2}{12}}$ <p><math>x = R\,1\,673,67</math>          a better option because monthly repayments are less.</p>	<p>✓ substitution into formula          ✓ <math>i = \frac{0,2}{12}</math>          ✓ <math>n = 48</math>          ✓ answer (4)</p>
9.1.3	<p><math>1673,67 \times 48</math>  <math>= 80336,16</math>  <math>80336,16 = 55000(1 + 4i)</math>  <math>1,460657455... = 1 + 4i</math>  <math>i = 0,11516436...</math>          Rate = 11,52%</p>	<p>✓ 80336,16          ✓  <math>80336,16 = 55000(1 + 4i)</math></p> <p>✓ answer (3)</p>
9.2	$80000 = \frac{25000 \left[ 1 - (1 + 0,1375)^{-n} \right]}{0,1375}$ $\frac{11}{25} = 1 - (1 + 0,1375)^{-n}$ $\frac{14}{25} = (1 + 0,1375)^{-n}$ $\log \frac{14}{25} = -n \log(1,1375)$ <p><math>n = 4,50054779</math>          The money will last for 4 full years</p> <p><b>OR</b></p> <p>Candidate guesses 4 years.          Then balance available at the end of 4 years (after the 4<sup>th</sup> withdrawal) is</p> $80000(1 + 0,1375)^4 - 25000 \left( \frac{(1 + 0,1375)^4 - 1}{0,1375} \right) = R11354,86.$ <p>At the end of the 5<sup>th</sup> year cannot have grown to R25000.</p>	<p>✓ substitution into correct formula          ✓ simplification</p> <p>✓ taking log of both sides</p> <p>✓ answer (4)</p> <p>✓ guesses 4 years</p> <p>✓✓ calculates balance at end of 4<sup>th</sup> year</p> <p>✓ conclusion about balance. (4)</p>



**QUESTION 10**

10.1	$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{\frac{1}{x+h} - \frac{1}{x}}{h}$ $= \lim_{h \rightarrow 0} \frac{x - (x+h)}{x(x+h)h}$ $= \lim_{h \rightarrow 0} \frac{-h}{x(x+h)} \times \frac{1}{h}$ $= \lim_{h \rightarrow 0} -\frac{1}{x(x+h)}$ $= -\frac{1}{x^2}$	<p>✓ substitution into correct formula</p> <p>✓ expansion</p> <p>✓ simplification</p> <p>✓ answer (4)</p>
10.2	$y = (2 - 5x)^2$ $y = 4 - 20x + 25x^2$ $\frac{dy}{dx} = -20 + 50x$ <p><b>OR</b></p> $y = (2 - 5x)^2$ <p>By the chain rule</p> $\frac{dy}{dx} = (2)(2 - 5x)(-5)$ $= -20 + 50x$	<p>✓ simplification</p> <p>✓✓ answers (3)</p> <p>✓ simplification</p> <p>✓✓ answers (3)</p> <p>[7]</p>

## QUESTION 11

11.1	$0 = x - 2$ $x = 2$ A(2 ; 0)	✓ answer (1)
11.2	$f(-1) = 0: -a + c = 2$ $f(2) = 0: 8a - 2c = 2$ $a = 1, c = 3$  <b>OR</b>  $a(x+1)(x+1)(x-2) = 0$ $a(0+1)(0+1)(0-2) = -2$ $-2a = -2$ $a = 1$ $f(x) = (x^2 + 2x + 1)(x - 2)$ $= x^3 - 3x - 2$  $c = -3$	✓ $-a + c = 2$ ✓ $8a - 2c = 2$ ✓ $a = 1$ ✓ $c = 3$  ✓ factors ✓ substitution  ✓ $a$ ✓ $c = -3$ (4)
11.3	$f'(x) = 0$ $3x^2 - 3 = 0$ $x^2 - 1 = 0$ $(x+1)(x-1) = 0$ B(1 ; -4)	✓ $f'(x) = 0$ ✓ $x^2 - 1$  ✓ answer (3)
11.4	$x - 2 = x^3 - 3x - 2$ $0 = x^3 - 4x$ $0 = x(x^2 - 4)$ $0 = x(x - 2)(x + 2)$ $x_c = -2, y_c = (-2)^2 - 3(-2) - 2 = -4$ C(-2 ; -4) $m_{BC} = \frac{-4 - (-4)}{1 - (-2)}$ $= 0$ BC is parallel to the $x$ -axis.  <b>OR</b>  Following from C(-2 ; -4), B and C have the same $y$ -coordinate, viz. -4. So BC is parallel to the $x$ -axis.  <b>OR</b>	✓ equating $f$ and $g$ ✓ standard form  ✓ factors ✓ $x_c = -2$ ✓ $y_c = -4$  ✓ $m = 0$ ✓ conclusion (7)  (7)

	$(x-2) = (x-2)(x+1)^2$ $\therefore (x+1)^2 = 1$ for $x \neq 2$ $\therefore x+1 = \pm 1$ $\therefore x = 0$ or $x = -2$ $y = -4$	(7)
11.5	$f''(x) = 0$ $6x = 0$ $x = 0$	$\checkmark f''(x) = 0$ $\checkmark$ answer (2)
11.6	$k < -4$ or $k > 0$	$\checkmark\checkmark$ answer $\checkmark$ or (3)
11.7	$f'(x) < 0$ $-1 < x < 1$ <b>OR</b> $3(x^2 - 1) < 0$ if $(x+1)(x-1) < 0$ $-1 < x < 1$	$\checkmark\checkmark$ answer (2) $\checkmark\checkmark$ answer (2) <b>[22]</b>

**This alternative memo must be used for students who follow through using  $c = -3$ . This marking memo must be used independently of the one provided in the existing memorandum.**

### QUESTION 11

11.1	$0 = x - 2$ $x = 2$ A(2 : 0)	$\checkmark$ answer (1)
11.2	$f'(-1) = 0; -a + c = 2$ $f(2) = 0; 8a - 2c = 2$	$\checkmark\checkmark f'(-1) = 0; -a + c = 2$ $\checkmark\checkmark f(2) = 0; 8a - 2c = 2$ (4)
11.3	$f(x) = x^2 + 3x - 2$ $f'(x) = 0$ $3x^2 + 3 = 0$	$\checkmark\checkmark f'(x) = 0$ $\checkmark 3x^2 + 3 = 0$ (3)

11.4	<p><b>If not attempted ( 3 marks)</b></p> <p><b>OR</b></p> <p>To calculate C</p> $x - 2 = x^3 + 3x - 2$ $x^3 + 2x = 0$ $x(x^2 + 2) = 0$ $x = 0$ $y = -2$	$\checkmark \checkmark \checkmark x - 2 = x^3 + 3x - 2$ $\checkmark x^3 + 2x = 0$ $\checkmark x(x^2 + 2) = 0$ $\checkmark x = 0$ $\checkmark y = -2$ <p style="text-align: right;">(7)</p>
11.5	$x = 0$ ( any method used)	$\checkmark \checkmark$ answer (2)
11.6	<p><b>Not Attempted : 0 marks</b></p> <p>OR</p> $k > 0$	$\checkmark \checkmark \checkmark$ answer (3)
11.7	<p>If <math>x &gt; -1</math>, <b>Maximum of 1 Mark</b></p> <p><b>OR</b></p> <p><math>x</math> is between -1 and (<math>x</math> – value ) of B</p> $f(x) = x^3 + 3x - 2$ $f'(x) = 3x^2 + 3 < 0$	$\checkmark \checkmark f'(x) = 3x^2 + 3 < 0$ <p style="text-align: right;">(2) <b>[22]</b></p>



**QUESTION 12**

12.1	Length of sides of square = $\frac{4-x}{4} = 1 - \frac{x}{4}$	✓ answer (1)
12.2	$x = 2\pi r$ $r = \frac{x}{2\pi}$ $\text{Areas} = \left(\frac{4-x}{4}\right)^2 + \pi\left(\frac{x}{2\pi}\right)^2$ $= \frac{16-8x+x^2}{16} + \frac{x^2}{4\pi}$ $= 1 - \frac{1}{2}x + \left(\frac{1}{16} + \frac{1}{4\pi}\right)x^2$ <p><b>OR</b></p> $x = 2\pi r$ $r = \frac{x}{2\pi}$ $\left(1 - \frac{x}{4}\right)^2 + \pi\left(\frac{x}{2\pi}\right)^2$ $1 - \frac{1}{2}x + \frac{x^2}{16} + \frac{x^2}{4\pi}$ $1 - \frac{1}{2}x + \left(\frac{\pi+4}{16\pi}\right)x^2$	✓ $r = \frac{x}{2\pi}$ ✓ sum of areas ✓ simplification ✓ simplification (4) ✓ $r$ ✓ sum of areas ✓ simplification ✓ simplification (4)
12.3	$x = \frac{-b}{2a}$ $= \frac{1}{2\left(\frac{\pi+4}{16\pi}\right)}$ $= 1,76 \text{ meter}$ <p><b>OR</b></p>	✓✓ substitution ✓ answer (3)

	$f(x) = 1 - \frac{1}{2}x + \frac{x^2(\pi + 4)}{16\pi}$ $f'(x) = 0 = -\frac{1}{2} + \frac{\pi + 4}{8\pi}x$ $4\pi = (\pi + 4)x$ $x = \frac{4\pi}{\pi + 4}$ $x = 1,76 \text{ m for the circle and } 2,24 \text{ m for the square}$	$\checkmark f'(x) = \frac{1}{2} + \frac{\pi + 4}{8\pi}x$ $\checkmark f'(x) = 0$  $\checkmark \text{ answer}$  <b>[8]</b>
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**QUESTION 13**

13.1	$4x + 2y \leq 32 \quad \therefore y \leq -2x + 16$ $2x + 4y \leq 36 \quad \therefore y \leq -\frac{x}{2} + 9$ $x + y \leq 10 \quad \therefore y \leq -x + 10$	$\checkmark \text{ answer}$ $\checkmark \text{ answer}$ $\checkmark \text{ answer}$  <b>(3)</b>
13.2	Attached graph	$\checkmark y = -2x + 16$ $\checkmark y = -\frac{x}{2} + 9$ $\checkmark y = -x + 10$ $\checkmark \text{ feasible region}$  <b>(4)</b>
13.3	$P = 60x + 80y$	$\checkmark \text{ answer}$  <b>(1)</b>
13.4	$80y = -60x + P$ $y = -\frac{3}{4}x + \frac{P}{80}$ <p>Maximum profit at (2; 8)</p> <p><math>\therefore</math> Grade 10: 2 learners must be trained to give a maximum profit</p> <p>Grade 11: 8 learners must be trained to give a maximum profit</p>	<p>13.4</p> $\checkmark \text{ search line}$  $\checkmark \checkmark (2; 8)$  <b>(3)</b>
13.5	$m = -\frac{4}{3}$ <p>Since the gradient of the new profit function is not equal to the gradient of the initial profit function, the new maximum point is (6 ; 4) that gives an optimal solution.</p>	$\checkmark m = -\frac{4}{3}$ $\checkmark (6; 4)$  <b>(2)</b>

**[13]**

**QUESTION 13.2 & 13.4**

